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Velocity/Pressure Response Curve Characterization of the Arterial Path of the P3 Iliac Reflection During Hemorrhage Simulation

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Abstract

Background: Recent work suggests that pulse pressure may be a marker of temporal changes in central blood volume, facilitating the non-invasive detection hemorrhage and the onset of hemorrhagic shock. A new approach to tracking blood pressure, and pulse pressure specifically is presented that is based on a new form

of pulse pressure wave analysis called Pulse Decomposition Analysis (PDA). The premise of the PDA model is that the peripheral arterial pressure pulse is a superposition of five individual component pressure pulses, the first of which is due to the left ventricular ejection from the heart while the remaining component pressure pulses are reflections and re-reflections that originate from only two reflection sites within the central arteries. The hypothesis examined here is that the PDA parameter T13, the timing delay between the first and third component pulses, correlates with pulse pressure. Furthermore the comparison of experimental and model predictions provides insight into the pressure/velocity responses of the different arterial segments that the iliac reflection pulse (P3) traverses.

T13 was monitored along with blood pressure, as determined by an automatic cuff and another continuous blood pressure monitor, during the course of lower body negative pressure (LBNP) sessions involving four stages, -15 mmHg, -30 mmHg, -45 mmHg, and -60 mmHg, in fifteen subjects (average age: 24.4 years, SD: 3.0 years; average height: 168.6 cm, SD: 8.0 cm; average weight: 64.0 kg, SD: 9.1 kg).

Results: Statistically significant correlations between T13 and pulse pressure as well as the ability of T13 to resolve the effects of different LBNP stages were established. Experimental T13 values were compared with predictions of the PDA model. These predictions revealed distinctly different response characteristics for the three major arterial segments that constitute the path of the P3 component pulse. The LBNP interventions resulted in pulse pressure changes of up to 7.8 mmHg (SE = 3.49 mmHg) as determined by the automatic cuff. Corresponding changes in T13 were a shortening by -72 milliseconds (SE = 4.17 milliseconds). In contrast to the other two methodologies, T13 was able to resolve the effects of the two least negative pressure stages with significance set at $p < 0.01$.

Conclusions: The agreement of observations and measurements provides a preliminary validation of the PDA model regarding the origin of the arterial pressure pulse reflections. The proposed physical picture of the PDA model is attractive because it identifies the contributions of distinct reflecting arterial tree components to the peripheral pressure pulse envelope. The results presented here suggest that the model may also be able to provide insight into the dynamic response characteristics of certain arterial tree sections, with important implication for the assessment of their health.

Keywords: Hemorrhage, Arterial Pulse Analysis, Pulse Decomposition Analysis, Pulse Pressure.

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1 Introduction

The objective of this work is the introduction of a new form of pulse pressure wave analysis, called Pulse Decomposition Analysis (PDA). As evidenced by the number of different

commercial and academic efforts, pulse analysis already provides access to the tracking of some cardiovascular parameters, such as cardiac output, left ventricular ejection etc. that are otherwise accessible only via either invasive means or sophisticated but also cumbersome monitoring modalities. As the work presented here suggests, a further refined pulse analysis model holds the promise of providing 1. access to additional vascular parameters and, perhaps equally important, their dynamic response characteristics and 2. the tracking of blood pressure without the physically restrictively engaging, and consequently uncomfortable, approaches that current continuous blood pressure monitors employ. Of particular interest in the context of tracking blood pressure is pulse pressure, the motivation being that pulse pressure appears to be a sensitive as well as specific marker for the detection of hemorrhage, [1-2] which remains one of the leading causes of death on the battlefield as well as in civilian trauma cases while also being highly preventable if intervention can be implemented [3-4]. However, detecting progressive hemorrhage requires resolution of changes on the order of a few mmHg in pulse pressures of, normally, 35-50 mmHg. Given the separate and unequal uncertainties in determining systole and diastole, using the best brachial cuff techniques, [5] such determinations are by and large out of reach even in controlled environments.

In response we present here the PDA approach, which not only offers the capability to continuously track blood pressure but to also provide insight into the response characteristics of certain arterial tree segments. The analysis of the arterial pressure pulse has been the subject of many studies, with works whose results are still relevant today dating from the 1800s and the early 1900s, [6-8] as well as a significant body of work that has been published over the past 40 or so years [9-16]. PDA presents the extension of the findings of a number of studies that have utilized ballistocardiography and invasive central artery manometers to track mechanical events such as heart contractions and pressure pulse reflections in the central arterial tree, to the arterial periphery. These studies [17-19] have confirmed the existence of two major reflection sites in the central arteries. The first reflection site is the juncture between thoracic and abdominal aorta, which is marked by a significant decrease in diameter and a change in elasticity and the second site arises from the juncture between abdominal aorta and common iliac arteries. In what follows these reflection sites are respectively referred to as the *renal* and the *iliac* reflection site. A consequence of these reflection sites are reflected arterial pressure pulses that counter-propagate to the direction of the single arterial pressure pulse, due to left ventricular contraction, that gave rise to them. Referring to Fig. 1, the *downward* traveling primary pressure pulse # 1 gives rise to the *upward* traveling # 2 and # 3 pulses that are respectively due to the renal and the iliac reflection sites on which the # 1 pulse impinged.

As these reflected # 2 and # 3 pressure pulses reach the aortic arch, they will enter the subclavian arteries and head into the arterial periphery of the arm, following the # 1 pressure pulse that, besides traveling down the aorta, also entered the arm complex arteries. The # 2 and # 3 pulses will do so with certain time delays because of the *extra* traversal of the central arteries.

The # 2 pulse is commonly known as the *second systolic* peak. We refer to it as the *renal reflection* and it follows the primary ejection pulse (# 1) into the arterial periphery of the arm at delays of between 70-140 milliseconds. The pulse labeled # 3 in Fig. 1

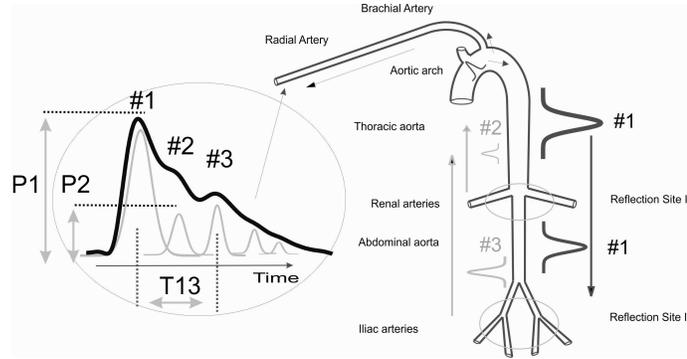


Figure 1: Sketch of the aorta/arm complex arterial system and its effect on the arterial pressure pulse line shape that is observed at the radial/digital artery. Two reflection sites, one at the height of the renal arteries, the other one in the vicinity of the iliac bifurcation, give rise to the reflected pulses (gray) that trail the primary left ventricular ejection (black). (from [31]).

is the much larger *iliac reflection*, which follows the # 1 pulse at delays of 180 to 400 milliseconds.

The described scenario succinctly explains the presence of three component pulses in the pressure pulse envelope that is observed in the arterial periphery of the arm, such as at the radial or digital arteries. In fact, there are additional component pulses. The presence of re-reflections between the central reflection sites has been previously suggested [20]. The physical picture is one where the iliac reflection pulse, in its travel up the aorta, re-reflects off the renal reflection site, and this re-re-reflection traveling downward, once again reflects off the iliac reflection site to follow the first three components pulses. With dramatically diminishing amplitude the scenario repeats for the fifth component pulse. These higher-order reflections are less relevant for quantitative analysis due to their poorer signal to noise characteristics and the fact that they are easily swallowed by the pulse envelope of the next cardiac cycle unless the heart rate is very low.

Based on these considerations the structure of the radial/digital arterial pressure pulse can be explained entirely by the interaction of the primary left ventricular ejection pressure pulse with two aortic reflection sites. We now hypothesize that it is possible to determine trends in aortic blood pressure through an analysis of the pulse envelope obtained in the arterial periphery of the arm.

The PDA model presented here analyzes the arterial pulse as observed on the lower arm by isolating, identifying and quantifying the temporal positions and amplitudes of the renal reflection pulse (# 2) and the iliac reflection pulse (# 3), each relative to the primary systolic pulse (# 1), within the pulse shape envelope of an individual cardiac cycle. The models predictions and experimental studies show that two pulse parameters are of particular importance. One parameter is the ratio of the amplitude of the renal reflection pulse (# 2) to that of the primary systolic pulse (# 1). These amplitudes, labeled P1 and P2, are indicated to the left of the arterial pressure pulse envelope. This parameter is herein referred to as the P2P1 ratio and it tracks changes in central beat-by-beat systolic pressure. The second parameter is the time difference between the arrival of

the primary systolic (# 1) pulse and the iliac reflection (# 3) pulse. This parameter is referred to as T13, as indicated in Fig. 1, and it tracks changes in arterial pulse pressure, also beat-by-beat.

It is the aim of this paper to validate the described arterial pressure pulse reflection scenario through the presentation of experimental data collected in the context of simulating central hemorrhage and its comparison with predictions of the PDA pulse propagation model. Specifically, our hypothesis is that the time delay between the primary component pulse (# 1) and the iliac reflection pulse (# 3), T13, correlates with pulse pressure.

We report here the results of monitoring the evolution of the PDA parameter T13 during the course of lower body negative pressure (LBNP) sessions. LBNP is an established technique used to physiologically stress the cardiovascular system. It has been used to simulate gravitational stress and hemorrhage, alter preload, and to manipulate baroreceptors [21]. LBNP was chosen for this project because it has been shown to be very effective at modulating pulse pressure, thereby providing a means to validate the equivalent PDA arterial pulse parameter, T13.

2 Patients and Methods

After IRB approval, tests of the CareTaker system, which is the hardware implementation of the PDA model that is described in more detail below, were performed at the Cardiovascular Physiology Laboratory of the University of British Columbia on fifteen healthy volunteers (average age: 24.4 years, SD: 3.0 years; average height: 168.6 cm, SD: 8.0 cm; average weight: 64.0 kg, SD: 9.1 kg) whose lower bodies, from the height of the iliac crest downwards, were subjected to increasingly negative pressures. A number of studies have demonstrated that it is possible to simulate significant internal hemorrhage using LBNP. Negative pressures of 10 – 20 *mmHg* correspond to 400 to 550 *ml* of central blood loss, 20 – 40 *mmHg* correspond to 500 to 1000 *ml*, and negative pressures in excess of –40 *mmHg* correspond to blood losses exceeding 1000 *ml* [22].

The subjects were subjected to four stages of negative pressure, –15 *mmHg*, –30 *mmHg*, –45 *mmHg*, and –60 *mmHg*, each stage lasting typically about 12 minutes. The blood pressure was monitored with an automatic cuff (BP TRU Automated Non-Invasive Blood Pressure Monitor (model BPM-100), VSM MedTech Devices Inc.) set to record blood pressures every three minutes, resulting in typically four readings per LBNP setting as well as an Ohmeda 2300 Finapres, and a pulse oximeter (Ohmeda Biox 3740 Pulse Oximeter, BOC Health Care) monitored oxygen saturation. The CareTaker system collected arterial pulse shapes beat-by-beat via a finger cuff attached to the central phalange of the middle digit. Four subjects became presyncopal and could not complete the -60 mmHg LBNP stage.

2.1 CareTaker Device

The hardware platform that provides the arterial pulse signal for the PDA algorithms analysis is the Care-Taker device (Empirical Technologies Corporation, Charlottesville, Virginia). It is a physiological sensing system whose three basic physical components are

a sensing pad such as a finger cuff that couples to an arterial pressure point, a pressure line that pneumatically telemeters the pulsations, and a custom-designed piezo-electric pressure sensor that converts the pressure pulsations, using transimpedance amplification, into a voltage signal that can be measured, digitized, transmitted and recorded. The coupling to the artery is accomplished using palpation coupling, such as at the radial artery, or approximate hydrostatic coupling, such as at the digital arteries. The completely self-contained device wirelessly transmits its signal representing the arterial pulse to a PC computer using the Bluetooth protocol. The device is not occlusive as it operates at a coupling pressure of about 40 *mmHg*. Another important characteristic of the device is that the signal it provides, sampled at 512 *Hz*, is the time derivative of the arterial pulse signal. The derivative provides significant signal to noise advantage and lowers the resolution requirements for digital acquisition of the signal because the derivative eliminates signal offsets. Because of the short time constants associated with its implementation, it also offers very short recovery times after signal disruptions. That is, in the absence of offsets due to the differentiation, the signal is always clamped to the signal base line, which in turn allows for increased amplification. Consequently the full digitization range of the analog to digital converter (A/D) can be used for the signal amplitude, as opposed to signal amplitude plus offsets.

2.2 The PDA model

The existence of two distinct central pressure pulse reflection sites make it is possible to propose a simple model of the arterial paths that the primary pulse and its reflections traverse and to compare its predictions with observations regarding the relative arrival times of the different components pulses. The models equations, which have been presented elsewhere [31], predict the time of arrival of each individual component pulse, subject to the total distance that the pulse has traveled and the pressure-dependent pulse propagation velocity in each arterial segment. The pressure dependence of the pulse propagation velocity is implemented using the Moens-Korteweg [23] equation, which relates pressure and velocity.

Another critical feature of the model is that R2, the renal reflection coefficient, is dependent on systolic pressure. The motivation for this is based on the following consideration. As discussed, the renal reflection (P2 pulse) originates at the junction between thoracic and abdominal aorta, a junction that is characterized by a significant change in arterial diameter. Since the thoracic aorta is the softest artery in the body, as evidence by the fact that it exhibits the lowest pulse pressure propagation velocities (4 – 5 *m/s*) and much more extensible than the abdominal aorta, increasing peak pressure, or systole, will enlarge the diameter mismatch, giving rise to a more pronounced renal reflection pulse amplitude while falling systole will produce the opposite effect, an effect observed in manipulative experiments performed by Latham [17]. The critical insight then is that the amplitude of the renal reflection will increase relative to the amplitude of the primary systolic (P1 pulse) peak because, while both component pulses travel the arteries of the arm complex, and are therefore both subject to the pulse narrowing and heightening due to the taper and wall composition changes of the peripheral arteries, only the renal reflection will have sampled the pressure-induced aortic impedance mismatch changes. This

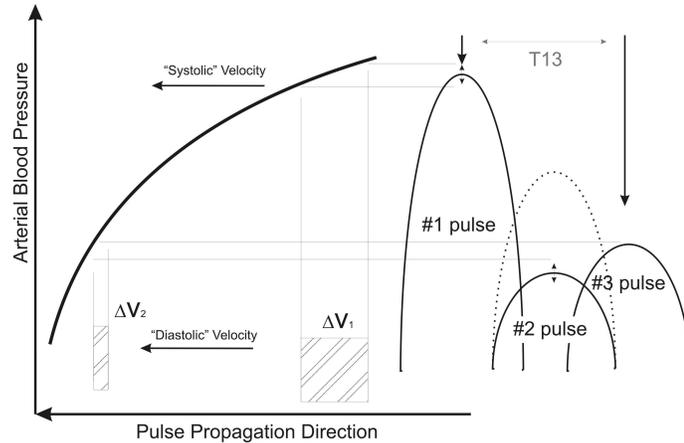


Figure 2: Relative amplitudes and velocity/pressure relationships of the component pulses. # 2's amplitude and propagation velocity can change significantly due to the pressure dependence of R_2 , the renal reflection coefficient. (from [31]).

establishes the motivation for taking the ratio of the amplitudes of the # 2 and the # 1 pulse, which is P2P1.

A similarly physical argument can be made for the difference in arrival times of the primary pulse (# 1) and the iliac reflection (# 3), or T13. The difference in the arrival times of the primary arterial pulse, that is the left ventricular ejection, and the iliac reflection pulse is determined by the differential velocities with which both pulses propagated along their arterial paths. In the case of the iliac reflection the path length is longer than that of the primary pulse by almost twice the length of the torso. More importantly, both pulses travel at different velocities because their pressure amplitudes are different. Specifically, the iliac reflection pulse amplitude, which is determined by the reflection coefficient of the iliac reflection site, is on the order of 40 percent of pulse pressure. This point is graphically made in Fig. 2, Both pulses therefore load the arterial wall differently during their arterial travel, as a result of which their propagation velocities are different. The second insight is that, because the pressure/velocity response curve is non-linear, a result known since the 1960s based on Anlikers work, [24] both pulses accelerate and decelerate at different rates as the pressure rises and falls. The primary pulse experiences the highest changes in velocity as a function of changes in blood pressure because it is subject to the steepest section of the pressure/ velocity response curve, while the iliac pulse, running at much lower pressure, changes velocity much more gradually. Changes in the time of arrival therefore then reflect changes in the differential arterial pressure that the two pulses experience. While this differential pressure is not exactly pulse pressure, that is the difference between the full pulse arterial pulse height and the diastolic pressure floor, it represents about 60-70 percent of it, assuming the previously stated iliac reflection coefficient.

Fig. 2, presents a graphic display of the relative amplitudes of the left ventricular ejection (# 1) and the trailing reflection pulses and their resulting relative positions on the pulse propagation velocity curve, which is highly pressure dependent. As a result the arrival times of the different pulses are highly pressure dependent, a point that is clarified

by Fig. 3, which presents the pulse travel times, from bottom to top, respectively, of the primary ejection pulse (# 1), the renal reflection (# 2), and the iliac reflection (# 3). The iliac pulses arrival time shortens only slightly with increasing pressure because its amplitude remains close to the diastolic pressure regime. The renal reflection peaks arrival time (middle) experiences significant non-linearity because the reflection coefficient, R_2 , is highly pressure dependent. The left ventricular ejection (# 1, bottom curve) has the highest amplitude and samples the steepest section of the pressure/velocity curve and is therefore most pressure dependent. Using *Youngs moduli* obtained from the literature and letting the model fit R_2 as well as the velocities of the primary arterial path ways it is then possible to compare experimental data with model predictions.

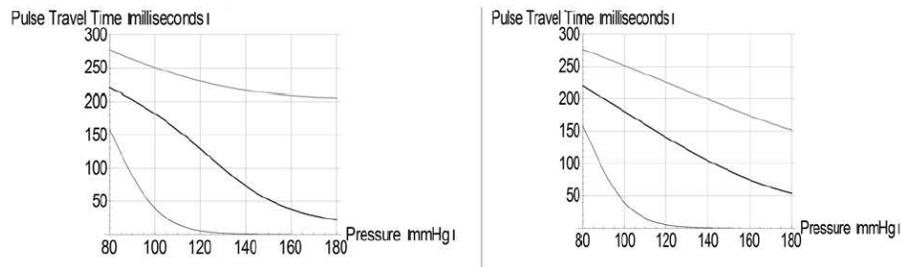


Figure 3: left graph (from [31]): Arrival times, as predicted by PDA model, of the three component pulses, from bottom up, # 1 (left ventricular ejection), # 2 (renal reflection), and # 3 (iliac reflection). Right graph: the effect of replacing the dynamic response of the renal reflection coefficient R_2 , shown in Fig. 12, with a constant reflection coefficient of 0.25.

Fig. 3, displays the fact that human arterial pathways, for the average height population we have studied, are generally very short relative the distances the arterial pulse traverses within a cardiac cycle. Typical arterial pulse propagation velocities range, for healthy and unstressed arteries, from 4 – 9 m/s . This fact influences particularly the arrival time of the # 1 pulse profoundly. In the lower pressure range, which is the pressure regime that was examined here, the # 1 pulse pulls away from the # 2 and # 3 reflection pulses, as evidenced by the fact that its arrival time shortens significantly faster with increasing pressure than the arrival times of # 2 and # 3. Consequently, in this pressure range, T13 would be expected to widen with increasing pressure and shorten with decreasing pressure. Fig. 3, therefore provides a quantitative basis for why T13 is hypothesized to be directly dependent on blood pressure changes in the blood pressure regime that was examined here.

As the pressure continues to increase, however, the arrival time of the primary # 1 pulse saturates as it runs out of arterial runway. Consequently further increases in arterial pulse propagation velocity do not result in a further shortening of the arrival time. Meanwhile the # 3 pulse continues to accelerate with increasing pressure, narrowing the T13 time delay in this high-pressure regime. The details of the pressure-dependent evolution of the arrival time curves are critically dependent on the choice of different velocity profiles for the different arterial sections, a point that is discussed later.

2.3 Pulse Decomposition Algorithm (PDA)

The algorithm that is based on the pulse analysis model just presented encompasses the following components:

1. A peak finder that identifies heartbeats in the derivative data stream.
2. A differentiator that produces the second derivative of the detected heart beat which is then used to find the inversions corresponding to the locations of the component pulses.
3. A digital integrator, implemented as a Bessel filter, that generates the integrated pulse wave form from the differentiated raw signal stream, and from which relative component pulse amplitudes are determined and 4. a low-pass filter that allows identification of the primary systolic peak. Furthermore the frequency content of the data stream is continuously analyzed in order to calculate signal to noise (S/N) figures of merit that determine whether signal fidelity is sufficiently high to permit peak detection and analysis.

The detection efficiency of the heart beats was typically on the order of 92 %, as evidenced by visual inspection of inter-beat spectra which readily reveal missed beats. Detection was typically poorest at the highest negative pressure (-60 mmHg) because of significantly diminished pulse amplitude.

Once the temporal locations of the reflection component pulses and the systolic peak are identified, the T13 interval, the time delay between systolic (P1) and iliac peak (P3), is calculated. The P2P1 ratio is calculated using the amplitudes of the P2 peak and the systolic peak, in the integrated pulse spectrum. Detection efficiency of the component pulses was on the order of 90 %. Detection again was poorest at the highest negative pressure because of diminished pulse amplitude.

2.4 Statistical Analysis

We present regression coefficients between LBNP levels and pulse pressure responses of the three measurement systems. In order to compare relative sensitivities of the three systems to changes in pulse pressure we present results of different repeated measures ANOVA analysis, which were performed using the Minitab statistical software (Release 14, Minitab Ltd.). Data are presented as means \pm SE unless specified otherwise.

3 Results

3.1 Comparison of Pulse Pressure Changes

In Fig. 4 we present an example of the evolution of arterial pressure pulse line shape changes for the 6 stages of an hour-long LBNP session (right-hand graph B) as well as the T13 trace for the entire session (left graph A). The subject in this case was a 31 y. female. The time evolution of the presented pulse line shapes is downward, starting at the top at atmospheric pressure, and ending with a pulse line shape obtained after

the LBNP chamber was vented from -60 mmHg back to atmospheric pressure. Each pulse line shape represents a 10-pulse average. The dynamic range of the iliac and renal

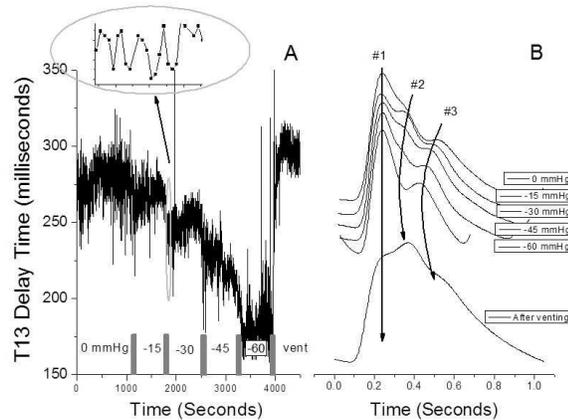


Figure 4: Relative amplitudes and velocity/pressure relationships of the component pulses. # 2's amplitude and propagation velocity can change significantly due to the pressure dependence of R2, the renal reflection coefficient. (from [31]).

peak positions is indicated by the downward sweeping arrows, while the position of the primary systolic peak (# 1) is indicated by the vertical solid arrow. The narrowing of the time interval between iliac and systolic component pulses with decreasing negative pressure is clearly visible. Furthermore, while the heart rate also changed, as indicated by the shortening inter-beat interval, it is clear that the rates of change for T13 and heart rate are different, i.e. the inter-beat interval narrowed faster than T13. A further point of interest is the shape of the arterial pressure pulse after venting, which in all subjects caused a significant rise in systolic blood pressure, as determined using the conventional blood pressure monitors. The pressure pulse line shape in question has the typical pulse shape associated with a positive augmentation index, which is defined as (height of # 2 pulse - height of # 1 pulse)/maximum overall amplitude [25]. A positive augmentation index is usually taken to be indicative of arterial aging, which, given the subjects age, is unlikely to be the case. This subjects pulse shape returned, along with normalizing systole, within minutes to the original line shape (top trace in Fig. 4B.)

While the results displayed in Fig. 4 exhibited a significant change in heart rate along with the change in T13, this was not a general observation. Figure 5 presents the results regarding inter-beat interval and T13 for subject # 9, a 24 y. male, who did not exhibit any appreciable change in heart rate until venting. The narrowing of T13 with decreasing negative pressure, however, matched those of all subjects.

Fig. 6 displays a representative side-by-side comparison of pulse pressures obtained with the automatic cuff (left graph) and the Finapres (center graph), as well as the evolution of the T13 parameter over the course of the LBNP session of subject # 3, (right graph). The general absence of a discernible trend in the readings of the cuff with progressing hypovolemia was typical for all data runs.

Fig. 7 presents comparative overall results for pulse pressures and T13 as a function of progressive decreasing negative pressure. Specifically, Fig. 7A presents the overall pulse

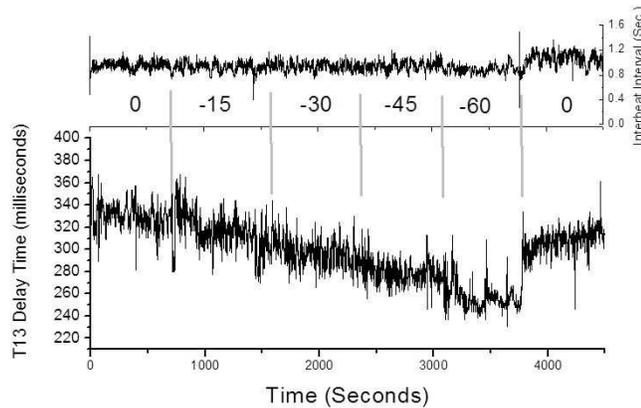


Figure 5: Temporal evolution of the inter-beat interval and T13 over the course of the LBNP session of subject # 9, 24 y. m., In this subject the narrowing of T13 was observed without any change in heart rate until venting. (from [31]).

pressure results of the automatic pressure cuff while Fig. 7B presents the overall results for T13. Fig. 7C. presents overall pulse pressure results for the Finapres.

The ability of the four measurement methods to resolve the effects of the different LBNP stages at a statistically significant level varied. While the PDA T13 parameter was able to resolve each of the four LBNP stages relative to atmospheric pressure, neither the Finapres nor the cuff were able to resolve the stages with the two least negative pressures (-15 & -30 $mmHg$), corresponding to the smallest changes in pulse pressure, with significance set at $p < 0.01$. Heart rate, as a detection modality for resolving the two least negative pressure LBNP stages, almost reached statistical significance, performing significantly better than the Finapres or the cuff. Table 1 presents the results of the ANOVA analysis.

Table 1: ANOVA: PDA, Finapres, Cuff versus LBNP (-15 & -30 $mmHg$)

Methodology	Significance
PDA - T13	0.00001
Finapres pulse pressure	0.636
Cuff pulse pressure	0.214
Heart rate (Finapres)	0.02

A receiver operating characteristic (ROC) analysis of the intra-subject ability of the four methodologies to resolve LBNP-induced differences of -15 $mmHg$ and atmospheric pressure, and -30 $mmHg$ and atmospheric pressure revealed similar differences. In Fig. 8 we present the results.

An important question is whether T13 is indeed a pulse pressure equivalent or whether it simply tracks the changes in heart rate referred to in Fig. 4 and Fig. 9 presents a comparison of pulse pressure, as measured with the cuff, as a function of T13 and heart rate, as measured with the Finapres, as a function of T13. While T13 correlates linearly

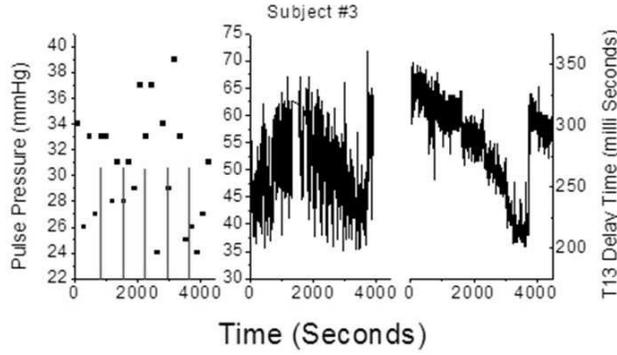


Figure 6: Comparison of the individual results for cuff-based pulse pressure (left graph), Finapres-based pulse pressure (center), and PDA-based T13 measurements, for subject # 3. The right panels present the simultaneously obtained T13 delay times between the primary left-ventricular ejection pulse and the iliac reflection pulse recorded on the subjects middle member of the middle digit. (from [31]).

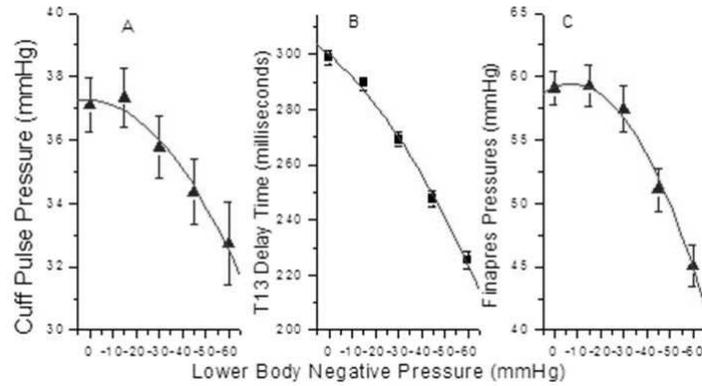


Figure 7: Overall results for pulse pressure obtained with the automatic cuff (graph A), the PDA pulse pressure-equivalent parameter T13 (B) and the Finapres (C). (from [31]).

with the pulse pressure determined using the cuff ($0.19\tilde{A} - T13$ (milliseconds) $+2.58$, $R2 = 0.98$, $p < 0.0001$) a second order model is required to obtain a correlation with heart rate ($-1.51 + T13$ (milliseconds) $\times 0.015 - 2.24526E - 5 \times T13E2$ (milliseconds)).

3.2 Comparison with model predictions

In Fig. 10 we present an overlay of the experimental results and the models predictions. The experimental data, all averages from 15 subjects, are the T13 values obtained from each LBNP stage as well as the corresponding pulse pressure values as determined with the Finapres. Since systole did not change appreciably for any of the subjects, we use the average value of 120 mmHg throughout. Consequently, as observed experimentally, changes in pulse pressure are driven entirely by changes in diastole. The most important aspect of the agreement between the model and data, as presented in Fig. 10, are the

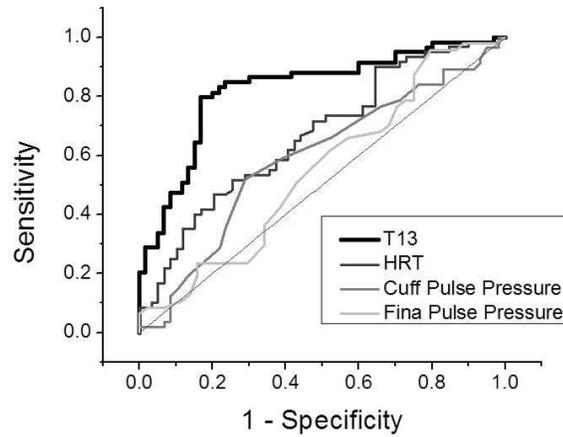


Figure 8: ROC analysis of the comparative intra-subject sensitivity/specificity of T13, heart rate, cuff pulse pressure, and Finapres pulse pressure to resolving the difference of -15 mmHg versus -30 mmHg LBNP relative to atmospheric pressure. Respectively the areas under the curve are 0.83, 0.66, 0.59, and 0.55. (from [31]).

arterial parameter assumptions that are required to achieve it. The single dominant factor that determines the response of T13 to pressure changes is the pressure/arterial pulse velocity response of the different arterial sections that the systolic pulse and its two central reflections traverse. Furthermore the range of relative pressure/velocity response curves that is possible, given the constraints of the experimental data, is very narrow. Fig. 11 presents the relative response curves of the three arterial segments that constitute the pulse pathways, the thoracic aorta, the abdominal aorta, and the arm complex arteries. Clearly the model at this stage uses a significant simplification of the arterial path sections and the response curves presented represent averages over these pathways. While more details will be introduced in future versions of the model the aim here is to demonstrate that the basic physical picture hypothesized by the PDA model matches observations. Fig. 12 displays the response characteristics of the reflection coefficient of the renal reflection site, as predicted by the model. While the starting values of the pressure/velocity curves for the arm complex arteries as well as the thoracic/abdominal aorta were based on published arterial pulse propagation velocities, [12] the results of the LBNP experiments provide an opportunity to deduce the relative dynamic response characteristics of the different sections, which are not readily available as they have not been the subject of research interests in a long time. In order to obtain the fit shown in Fig. 10, a different dynamic behavior of the arm complex relative to that of the central arteries had to be modeled. Specifically, while the arm complex arteries required a distinct exponential response characteristic, the simulated central arteries response, in the blood pressure range under consideration, was, in the case of the thoracic aorta, essentially linear and in the case of the abdominal aorta, of lower gain. These results are presented in Fig. 11. And it is this difference in dynamic response that enables the model to generate T13 curves whose slopes match those observed. In contrast, changes in starting values only shifted the family of curves in parallel up or down in but did not change the relative slopes of the curves.

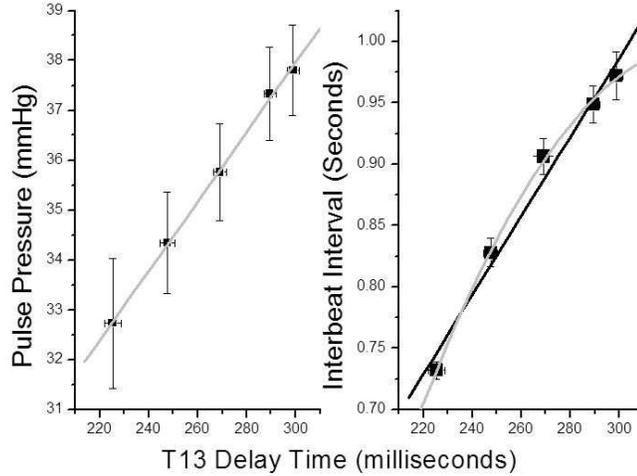


Figure 9: Functional comparison of T13 with pulse pressure obtained from cuff (left), and heart rate (right). (from [31]).

The other significant factor affecting the models prediction is the dynamic response curve of the renal reflection coefficient R_2 as a function of pressure (Fig. 12). Not surprisingly, the dynamic response of the reflection coefficient becomes increasingly important at higher pressures. The effect is clearly seen in the modification of the arrival time curves of the component pulses, which are presented in the two graphs of Fig. 3. The left graph corresponds to the arrival times with the R_2 having the pressure response characteristic shown in Fig. 12. The right graph displays the dramatically altered results, which would yield a very poor fit with the observed delay times, for a constant reflection coefficient of 0.25.

4 Discussion

Before discussing the implications of what appear to be statistically significant correlative results it is important to consider the hypothesis of whether they could be due to an unrelated experimental artifact, specifically the increasing abdominal compression with the increasing LBNP pressures that has been reported [26]. Two arguments can be made to refute this concern. If the increasing abdominal compression were to have progressively given rise to a new reflection site between renal and iliac reflection sites, a new reflected component pulse would have arisen between the # 2 and # 3 component pulses, progressively increasing with each LBNP-induced abdominal compression stage. Such additional central reflection sites have been observed by Kriz [20] in the context of aortic aneurysms. We have observed the resulting additional component pulses of such aortic aneurysms in the arterial periphery, a subject of future publication. However, as part of this work, in none of the LBNP stages and in none of the subjects studied were such additional component pulses observed.

A second argument is that the same response in T13 is observed in the case of actual

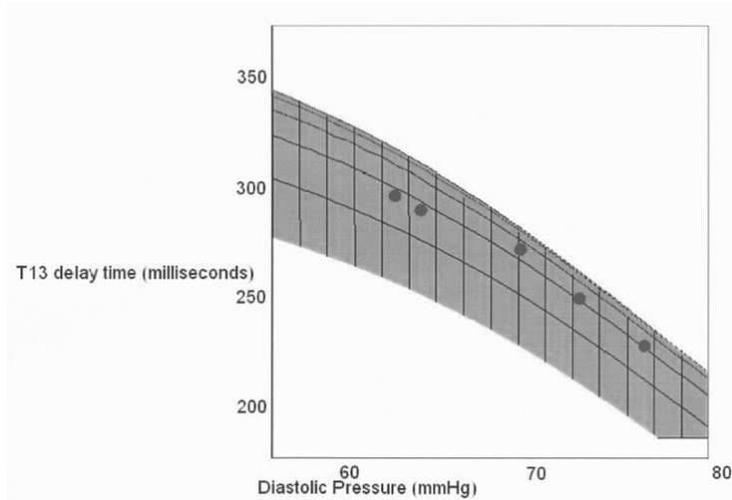


Figure 10: Overlap of PDA T13 prediction and LBNP study data as a function of diastolic pressure change. The line around which the data are grouped corresponds to systole = 120 mmHg. Adjacent lines correspond to ± 5 mmHg. (from [31]).

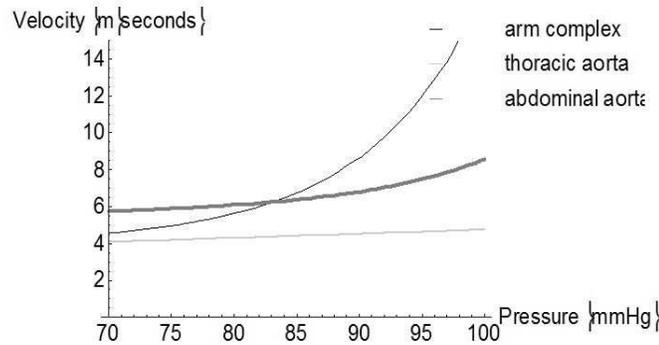


Figure 11: Arterial pulse velocity profiles as a function of pressure, based on fit to experimental results in Fig. 10.

hemorrhage, induced through blood donation of 1 *pint*. A just-completed study with 50 subjects, whose results will be published shortly, has confirmed the continuous decrease of T13 as the blood donation progressed. Moreover, the decrease observed in the blood donation experiment matched well the average decrease that was observed in the first stage (-15 mmHg) of the LBNP results reported here, in line with the estimation of central blood loss for that stage [22].

The results presented therefore support the hypothesis that the time delay between the primary component pulse (# 1) and the iliac reflection pulse (# 3), T13, correlates with pulse pressure and provide a first milestone in the validation of the PDA model. A number of conclusions follow.

Any reflection sites in the arm complex arteries proximal to the radial/digital arteries will not affect the pulse line shape that is observed there because any pulse reflections due

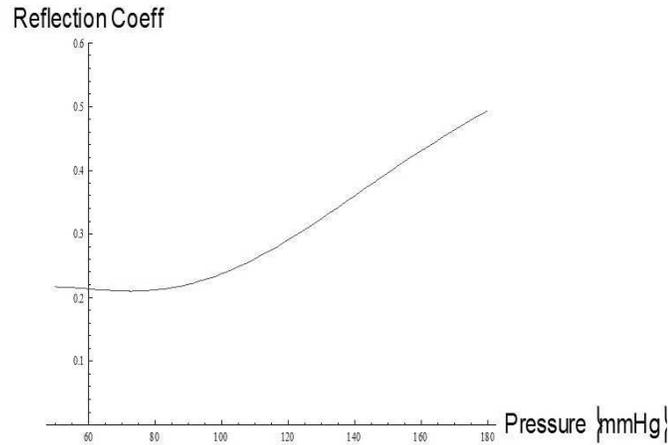


Figure 12: Pressure response of R2, reflection coefficient of the junction of thoracic/abdominal aortic sections at the height of the renal arteries.

to such reflection sites will travel away from them and back toward the central arteries. Their re-entry into the arm complex arteries could only be accomplished as re-reflections, with dramatically reduced amplitudes that would be masked by the primary renal and iliac reflections.

The hypothesis that the shape of the peripheral pressures pulse is predominantly determined by reflections in the aorta may seem surprising and will no doubt be gradually accepted. On the one hand maneuvers that are known to modify the thoracic pressure profile, such as valsalva that selectively modulates the renal reflection site and therefore the # 2 component pulse, [17] provide a ready method to demonstrate the critical importance of the central reflection sites. Alternatively manipulative experiments in the arterial periphery could be suggested to support or challenge the hypothesized physical picture. One possibility is partial occlusion of a femoral artery, with pulse monitoring distally on, for example, the pedal artery. Particularly since in the legs the # 2 and # 3 component pulses are diminished because they are re-reflections, it should be possible to observe the additional component pulse that would originate from the partial occlusion site, travel to the iliac reflection site and reflect there toward the distal monitoring site.

Movement of the occlusion site along the leg arteries should change the timing of the additional component pulse relative to the pulse envelope.

A relevant physiological phenomenon is pressure pulse amplification of the arterial periphery that is attributed to the taper of the arterial walls as well as their changing wall composition relative to the core arteries. The important realization here is that, while the arterial pressure pulse is temporally compressed and increased in amplitude, these changes to the pulse envelope are, in the absence of arterial dilation or constriction, static. This is the basis of using the validated transfer function approach [12] that uses pulse shapes obtained in the arterial periphery to predict central artery pulse shapes and blood pressures. It is the central artery dynamics that determine the peripheral pulse in the transfer function model. In the PDA model, which offers a concrete physical model instead of a generalized Fourier-based inverse filter, it is also the central artery dynamics that dominate the relationships between the components. Significant arterial dilation and

constriction does modify the component pulse relations, and this is an object of current study.

The differential pressure/velocity response curves predicted by the model for the different arterial sections that the iliac reflection pulse (# 3) traverses are not very surprising. The change-over from elastin, the main component of central artery walls [12] to the tougher collagen, which characterizes arterial wall content in the periphery, is well known. Consequently one would expect, particularly in the case of the thoracic aorta that has the slowest arterial pressure pulse propagation velocity (see starting value of 4.2 m/s), a much diminished increase in the velocity with rising pressure.

The regard to the changes in the arrival times of the component pulses (Fig. 3) with a change in the pressure response characteristic of the R2 (renal) reflection coefficient, this relation might at first appear surprising. The result is however less surprising after considering that the pressure response dynamic of R2 redistributes amplitude between the component pulses; in particular that it increases the P2 (renal) reflection pulse amplitude while reducing the P3 (iliac) pulse amplitude as the pressure rises. With lowered pressure amplitude, P3 travels slower than it would if it were not losing amplitude to P2 because of the pressure dependent R2 coefficient. The agreement with observed results consequently provides a rather compelling argument in support of the dynamic response of R2. The point was made earlier that the differential pressure between P1, the primary ejection pressure pulse, and P3, the iliac reflection pulse, is not exactly pulse pressure, that is the difference between the full pulse arterial height and the diastolic floor, but about 60 – 70 percent of it. Consequently the question arises how useful the differential pressure, which is reflected in the time interval T13, is in approximating pulse pressure. As clarified by Fig. 2, T13 corresponds to the pressure amplitude difference between the primary ejection pulse (# 1) and the iliac reflection (# 3). From the graph one readily sees that this amplitude difference covers exactly the most important part of the response curve that relates pressure to velocity, this being the exponential response section. The amplitude of the (# 3) pulse is entirely in the diastolic regime, which is linear, as Anliker showed. [32] However, it is the exponential section that is responsible for 95 percent of the dynamic pressure/velocity response characteristics, the rest being simply a linear offset.

The head plays a much diminished role in regard to pressure pulse reflections that are observed at the arterial periphery of the arm. Arterial pressure pulse reflections that return via the carotid arteries will, upon entering the aortic arch and traveling along the descending thoracic, re-reflect off the reflection site in the vicinity of the renal arteries. Assuming a reflection coefficient on the order of 17 percent, the amplitude of such a re-reflection will be on the order of 3 percent of the primary peak amplitude, and consequently be masked by the much larger pressure primary pulse reflections # 2 and # 3.

The PDA model ties together recent related observations by others. The fact that the ratio of the amplitudes of the # 2 (P2) and # 1 (P1) pulses correlates with systolic pressure is not surprising in light of the results obtained by Takazawa et. al., [27] Takada et. al., [28] and Imanaga et al. [29] In Fig. 13, which displays the 10-pulse average of the arterial digital pressure pulse of a 21 y. male athlete, we also present the second derivative of the arterial pulse. Takazawa et. al. labeled the different inversions, *waves*, of this second derivative trace as indicated in Fig. 13. The results of several studies suggest

that the ratio d/a correlates with blood pressure, along with many other physiological parameters [27-28]. Comparative inspection of the two traces establishes that the waves **a** and **d** are temporally in very similar positions to P1 and P2, respectively. A parameter introduced by Bartolotto [25] that incorporates very similar definitions of P1 and P2 as the PDA model was also found to correlate with systolic pressure. This parameter is the augmentation index of the photoplethysmograph, PTG (AUGI), and it is defined as $(P2 - P1)/MA$, where P2 and P1 are the amplitudes of the primary and second systolic peaks in the photoplethysmograph, respectively, and MA is the maximum envelope amplitude. These correlative results support the PDA model, which supplies the physical explanation both for the origin of the component pulses as well as why the correlation of the relative amplitudes of these component pulses with systolic pressure exists. As with the PDAs

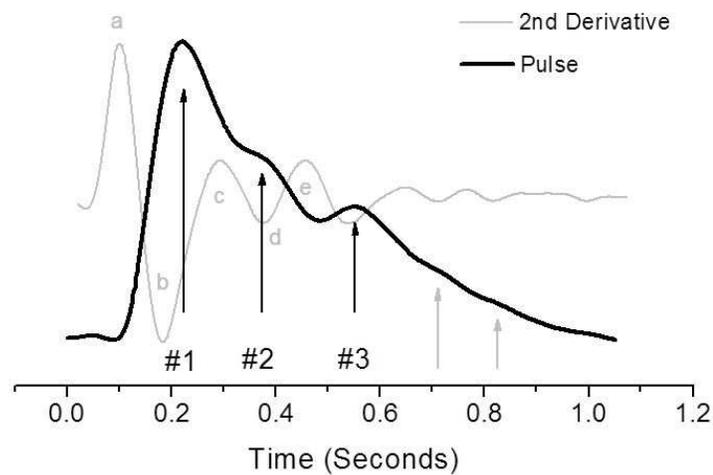


Figure 13: Arterial pressure pulse line shape (black trace, 10-pulse average), and its second derivative (gray trace), of a 21 y. male athlete collected at the middle phalange of the middle finger. The pulse line shape displays distinct pulsatile features labeled # 1, # 2, # 3. While the # 1 is the direct pass due to left ventricular ejection, the rest of the pulse envelope is due to arterial reflections. Indicative of distinct arterial pulse reflection sites is the fact that the reflected wave exhibits pulsatile components (# 2, # 3, and beyond) that feature comparable temporal extents as the primary ejection-related feature # 1. The inversions of the second derivative trace are labeled according to the convention introduced by Takada et. al. (from [31]).

P2P1 parameter, others have suggested measures that utilize the same time interval corresponding to T13 and have somewhat comparable physical interpretations. Millasseau [30] labels the time delay PPT in the digital volume pulse and suggests that it corresponds to the transit time of pressure waves from the root of the subclavian artery to the *apparent* site of reflection *in the lower body* and back to the subclavian artery. The reason for choosing the subclavian artery as a starting and ending point is however unclear, since the pressure wave does not originate there. If, on the other hand, the subclavian artery were to give rise to the # 3 pressure pulse as a reflection site, the amplitude of the iliac pulse would be dramatically lower than what is observed (20 – 40) percent of the primary

peak) at the radial or digital artery. Succinctly put, the pulse would have traveled from the left ventricle to the subclavian artery, reflected there at some reflection site, then to travel to the iliac reflection site. It would return from there as a re-reflection pulse with commensurately much reduced amplitude, an unlikely scenario.

A significant benefit of measuring T13 over pulse pressure directly is its higher resolution and sensitivity.

The results indicate the equivalence of a change of about 200 milliseconds in T13 to a variation of about 8 mmHg in pulse pressure over the entire range of a simulated central blood loss in excess of 1 liter for this cohort of fit and relatively young subjects. The results therefore indicate that the PDA technology is capable of resolving small changes in pulse pressure, a feat that sphygmomanometers are not well suited for. Given the suggestion by others that pulse pressure can be considered as a surrogate for stroke volume and therefore as a means to track loss of blood volume in trauma patients, [1] the accurate monitoring of pulse pressure could be a vital component in predicting hemorrhagic shock.

The potential benefits of utilizing T13 in detecting small changes in pulse pressure, coupled with the small size of the wireless CareTaker hardware, which weighs on the order of 5 oz, and the fact that it tracks blood pressure at low coupling pressures, makes the system attractive for the monitoring of patients at risk for internal hemorrhage. A benefit of such field-based monitoring is that internal hemorrhage could be detected well before hemodynamic collapse, making timely intervention feasible.

Currently studies are underway to further validate the PDA model by simultaneously correlating intra-aortic blood pressure with the peripherally measured PDA parameters T13 and P2P1.

5 Conclusions

We have presented a new physical model of the propagation of the arterial pressure pulse and its reflections as well as a comparison of the predictions of the model with experimentally obtained pulse parameters and conventionally obtained blood pressures. The agreement of observations and measurements provides a preliminary validation of the model which in turn could provide a renewed impetus in the study of the human arterial pressure pulse. The model is based on few, physical, assumptions because it proposes that the structure of the pulse is due to it is readily identifiable arterial pulse reflection sites. As a result it is also readily testable.

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